

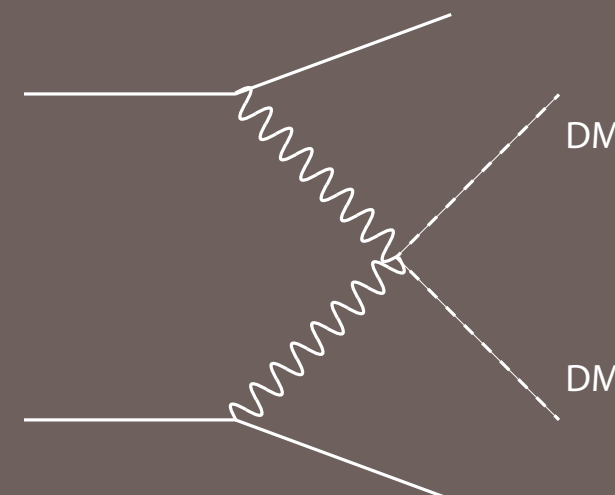
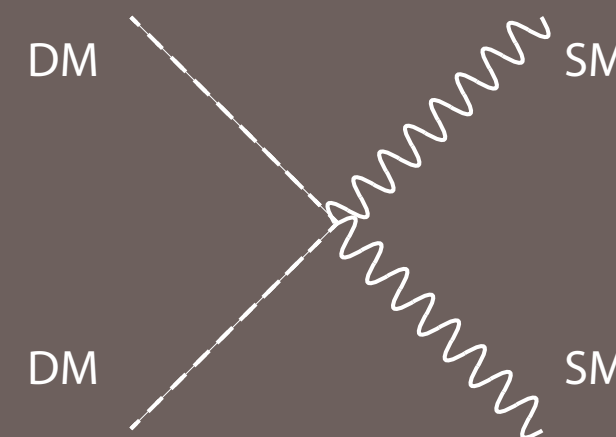
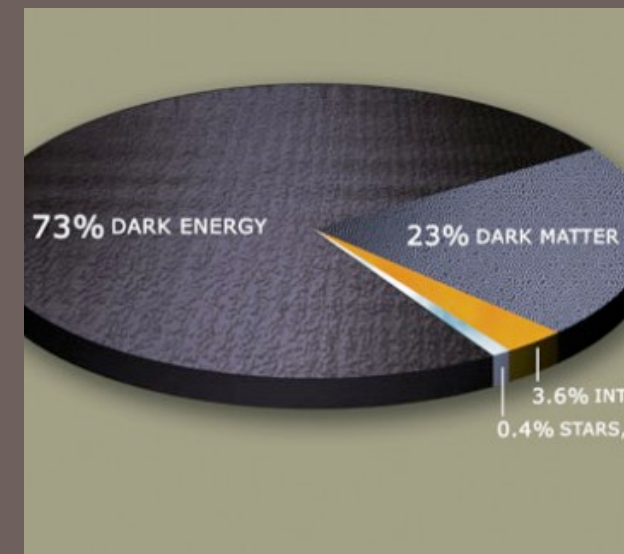
# A new take on dark matter in Little Higgs models

Alejandro de la Puente  
TRIUMF

Workshop on String Theory, Gravity and Fields,  
3rd Edition 2013

University of Buenos Aires  
Buenos Aires, Argentina

Based on arXiv:1304.7835  
In collaboration with Travis Martin, TRIUMF



- Collective Symmetry Breaking
- Motivation
- Dark Little Higgs Models
- Next to Littlest Higgs



# Collective Symmetry Breaking

- Little Higgs models are extensions of the Standard Model (SM) that stabilize the electroweak scale with a light Higgs boson.



# Collective Symmetry Breaking

- Little Higgs models are extensions of the Standard Model (SM) that stabilize the electroweak scale with a light Higgs boson.
- Fine tuning problem is solved by embedding the SM-like Higgs boson within a non-linear sigma field and introducing new heavy gauge bosons and fermions.



# Collective Symmetry Breaking

- Little Higgs models are extensions of the Standard Model (SM) that stabilize the electroweak scale with a light Higgs boson.
- Fine tuning problem is solved by embedding the SM Higgs boson within a non-linear sigma field and introducing new heavy gauge bosons and fermions.
- Scalar potential undergoes collective symmetry breaking → leads to cancellation of quadratic divergences.



# Collective Symmetry Breaking

- Toy Model:

- Broken Global Symmetry at a scale  $f$ :

$$SU(3) \rightarrow SU(2)$$

- Parametrize Nambu–Goldstone bosons (NGBs):

$$\Sigma(x) = \frac{1}{f} \exp \left( \frac{2i\pi^a(x) X^a}{f} \right) \Sigma_0 \quad \Sigma_0 = (0, 0, f)$$

- Dynamics are determined by:

$$\mathcal{L}_{\text{kin}} = f^2 \partial_\mu \Sigma^\dagger \partial^\mu \Sigma$$



# Collective Symmetry Breaking

- Toy Model:

- Would like to identify one of the NGBs with the SM-like Higgs boson... 4/5 degrees of freedom.
- Need to incorporate gauge interactions: This is done by gauging a subgroup of the full SU(3) symmetry:

$$\partial_\mu \rightarrow D_\mu = \partial_\mu - igW_\mu^a(x)Q^a$$

- Mass term and quartic self-interaction are radiatively generated:

$$\mu^2 \sim \frac{g^2}{16\pi^2}\Lambda^2, \quad \lambda \sim \frac{g^2}{f^2} \frac{1}{16\pi^2}\Lambda^2$$

- Theory valid up to  $\Lambda \sim 4\pi f$ .



# Collective Symmetry Breaking

- Toy Model:
  - A Higgs mass below 245 GeV requires  $f \sim 200\text{--}300$  GeV:  $\Lambda \sim 3 \text{ TeV}$
  - However EWPD requires  $\Lambda \sim 10 \text{ TeV}$ ... We now have a 125 GeV SM-like Higgs boson.
  - Can this toy model be modified such that one-loop quadratic divergent corrections to Higgs mass vanish?





# Collective Symmetry Breaking

- Toy Model:
  - Follow same idea of  $G/H$  breaking at a scale  $f$ :
  - However a subgroup  $G_1 \times G_2 \times \dots$  is gauged, each containing an  $SU(2) \times U(1)$  subgroup.
  - Furthermore each of the  $G_i$  commutes with a subgroup of  $G$  that acts non-linearly on the Higgs.
  - Full  $G_1 \times G_2 \times \dots$  needs to be gauged for SM-like Higgs boson to acquire a mass... Non-vanishing quantum corrections must be proportional to all gauge couplings.

# Little Higgs Models

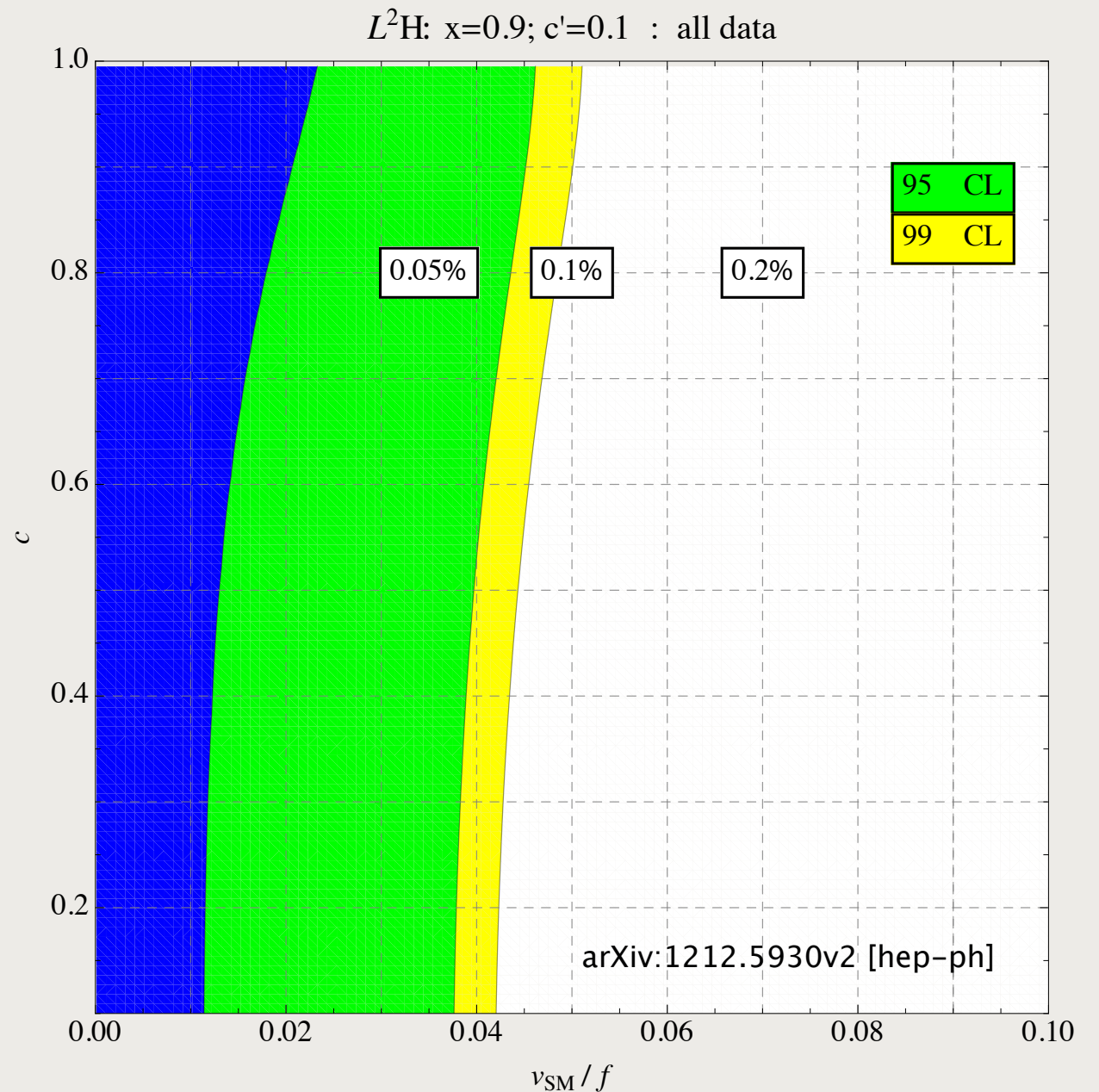
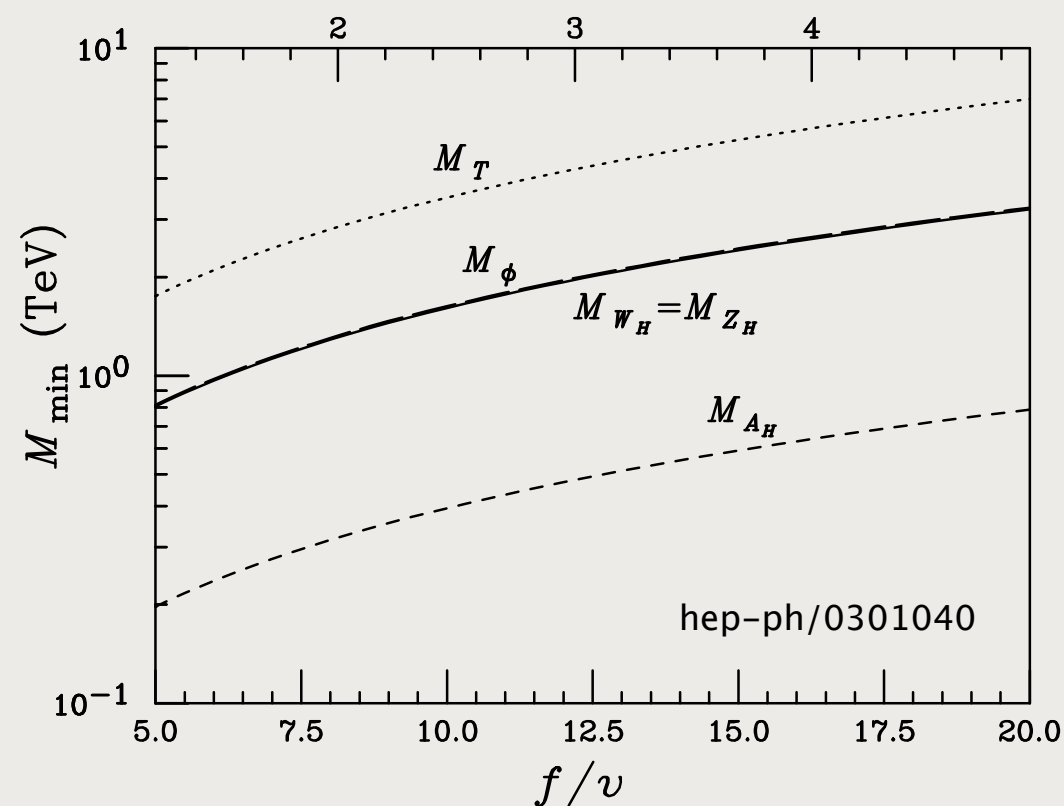
- Non-linear sigma model w/ collective symmetry breaking:  $SU(5)/SO(5)$
- New states cancel quadratic divergences
  - $t \leftrightarrow T$
  - $W/Z \leftrightarrow W'/Z'$
- EWSB induced from top loop contributions to Higgs mass

# Littlest Higgs Model

## ● Constraints

$$M_T \gtrsim m_t \frac{2f}{v}$$

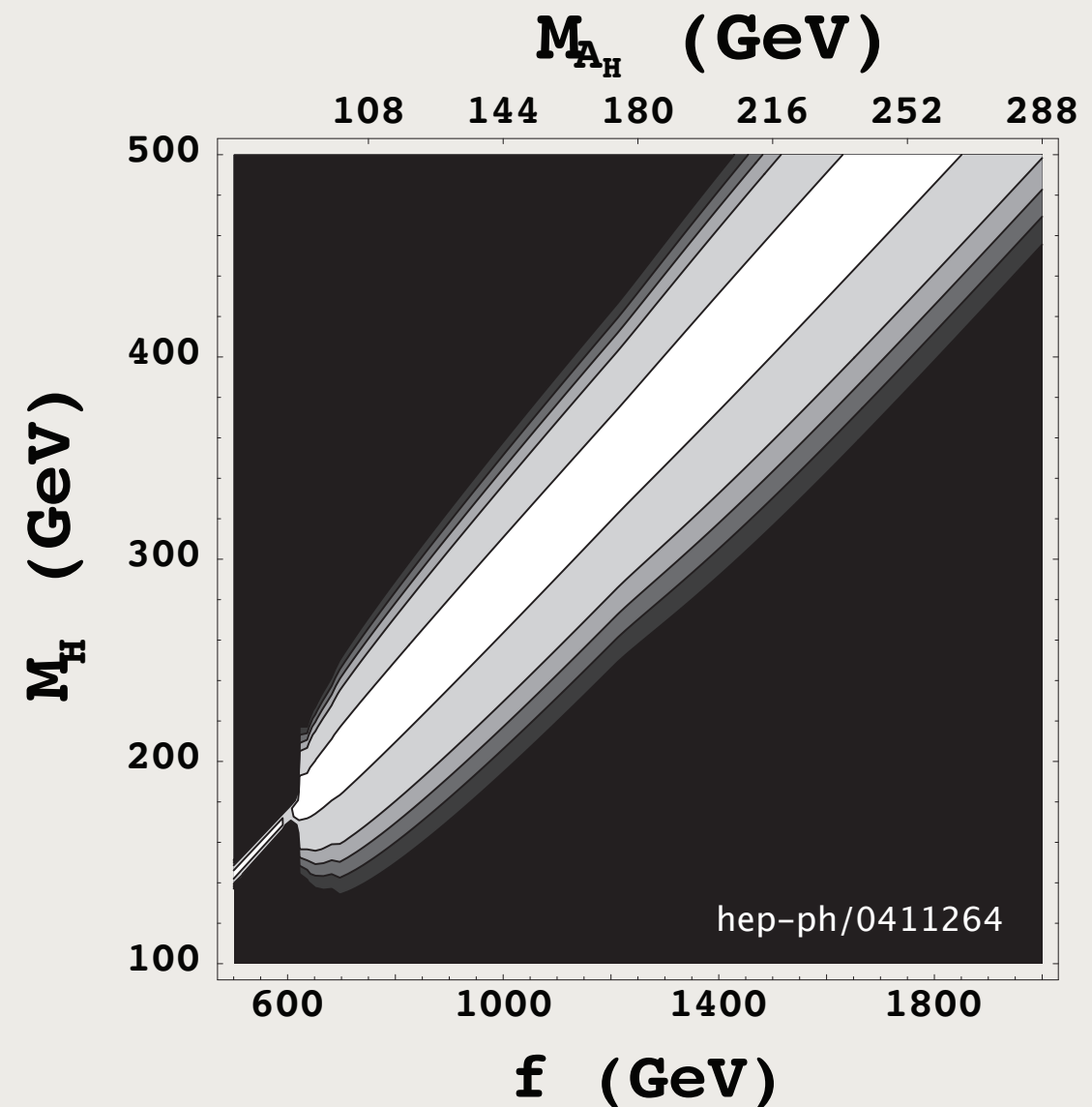
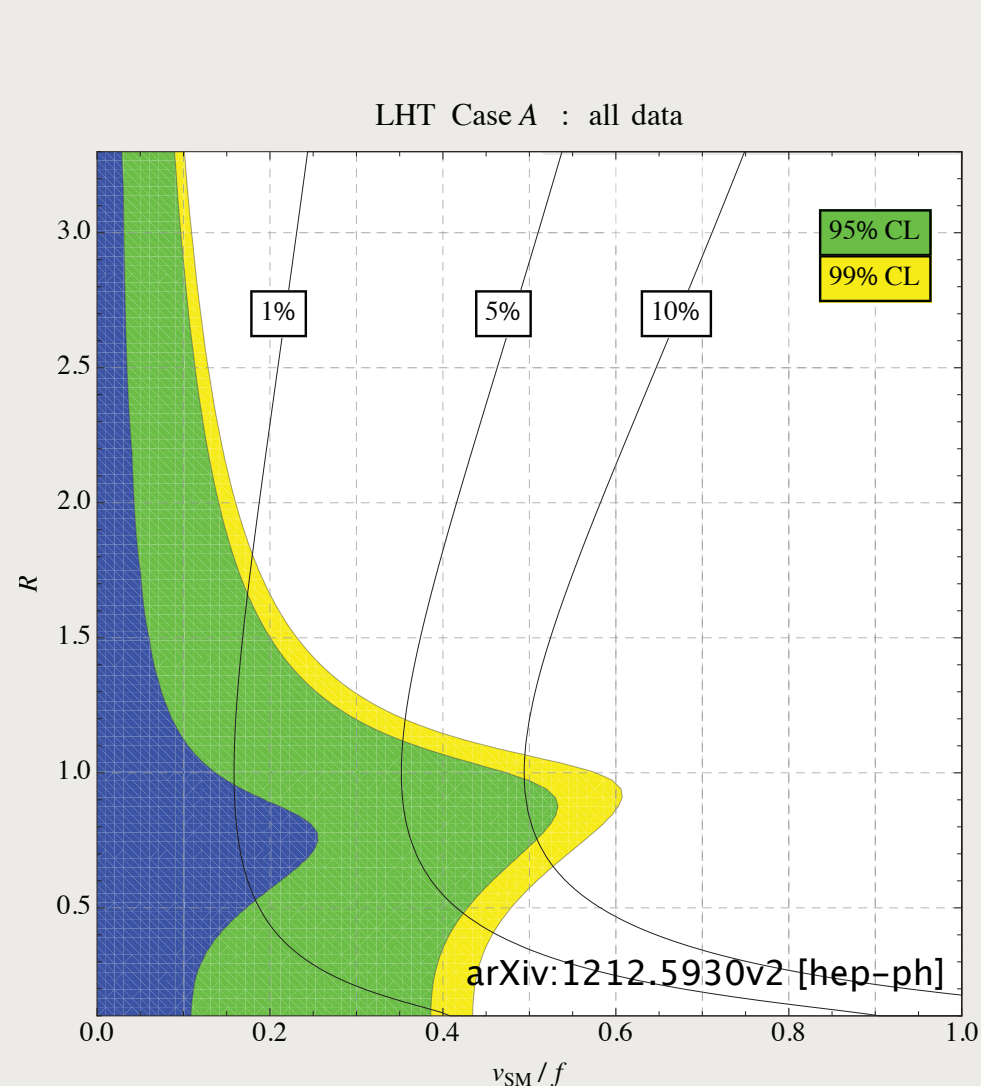
$$M_{W_H} \gtrsim m_W \frac{2f}{v}$$





# Littlest Higgs with T-Parity

- EWPO relaxed
- Light Higgs limits DM viability



# Dark Little Higgs

- Question: Can we resolve (some of) the constraints on the Littlest Higgs and introduce dark matter, all without introducing T-parity?
- Claim: Yes.

# Dark Little Higgs

- Separate  $W'$  and  $T$  masses.
- Little Higgs-ing the Inert Doublet Models.

# Dark Little Higgs

- Little Higgs-ing the Inert Doublet Models
- Separate  $W'$  and  $T$  masses: (arXiv:1006.1356)
  - Introduce second (duplicate) coset space
    - $G_S/H_S$  breaking at scale  $f$
    - $G_D/H_D$  breaking at scale  $F (>f)$
  - Both global symmetries gauged the same
  - Fermions transform only under  $H_S$
- $M_{W'}^2 \sim \text{Const.} (f^2 + F^2)$     $M_T^2 \sim \text{Const.} (f^2)$

# Next to Littlest Higgs

## ● $SU(5)_S/SO(5)_S$

$$\Pi_\Sigma = \begin{pmatrix} 0 & h^\dagger/\sqrt{2} & \phi^\dagger \\ h/\sqrt{2} & 0 & h^*/\sqrt{2} \\ f & h^\top/\sqrt{2} & 0 \end{pmatrix} + (Q_1^a - Q_2^a)\eta^a + \sqrt{5}(Y_1 - Y_2)\sigma$$

## $SU(5)_D/SO(5)_D$

$$\Pi_\Delta = \begin{pmatrix} 0 & \xi^\dagger/\sqrt{2} & \chi^\dagger \\ \xi/\sqrt{2} & 0 & \xi^*/\sqrt{2} \\ \chi & \xi^\top/\sqrt{2} & 0 \end{pmatrix} + (Q_1^a - Q_2^a)\alpha^a + \sqrt{5}(Y_1 - Y_2)\beta$$

$\Sigma$

---

2h doublets

2 h triplets

1  $\mathbb{R}$  triplet

1  $\mathbb{R}$  singlet

$h$      $\xi$

$\phi$      $\chi$

$\rightarrow \eta \leftarrow$  (a)

$\rightarrow \sigma \leftarrow$  (b)





# Next to Littlest Higgs

- Add to scalar kinetic terms

$$L_K = \frac{f^2}{8} \text{Tr} [(D_\mu \Sigma)(D^\mu \Sigma)^\dagger] + \frac{F^2}{8} \text{Tr} [(D_\mu \Delta)(D^\mu \Delta)^\dagger]$$

- Yukawa interactions unchanged

$$L_Y = \frac{1}{2} \lambda_1 f \epsilon_{ijk} \epsilon_{xy} \chi_i \Sigma_{jx} \Sigma_{ky} u_3'^c + \lambda_2 f \tilde{t} \tilde{t}'^c + \text{h.c.}$$

- Coleman–Weinberg potential

$$V_{CW} = \frac{\Lambda^2}{32\pi^2} \text{Str} [M^2(\Sigma, \Delta)] + \frac{1}{64\pi^2} \text{Str} [M^4(\Sigma, \Delta) \left( \log \left( \frac{M^2(\Sigma, \Delta)}{\Lambda^2} \right) - \frac{1}{2} \right)]$$

# Dark Matter Mass Splitting

$$V = \mu_1^2 |H_1|^2 + \mu_2^2 |H_2|^2 + \lambda_1 |H_1|^4 + \lambda_2 |H_2|^4 \\ + \lambda_3 |H_1|^2 |H_2|^2 + \lambda_4 |H_1^\dagger H_2|^2 + \lambda_5 \text{Re} [(H_1^\dagger H_2)^2]$$

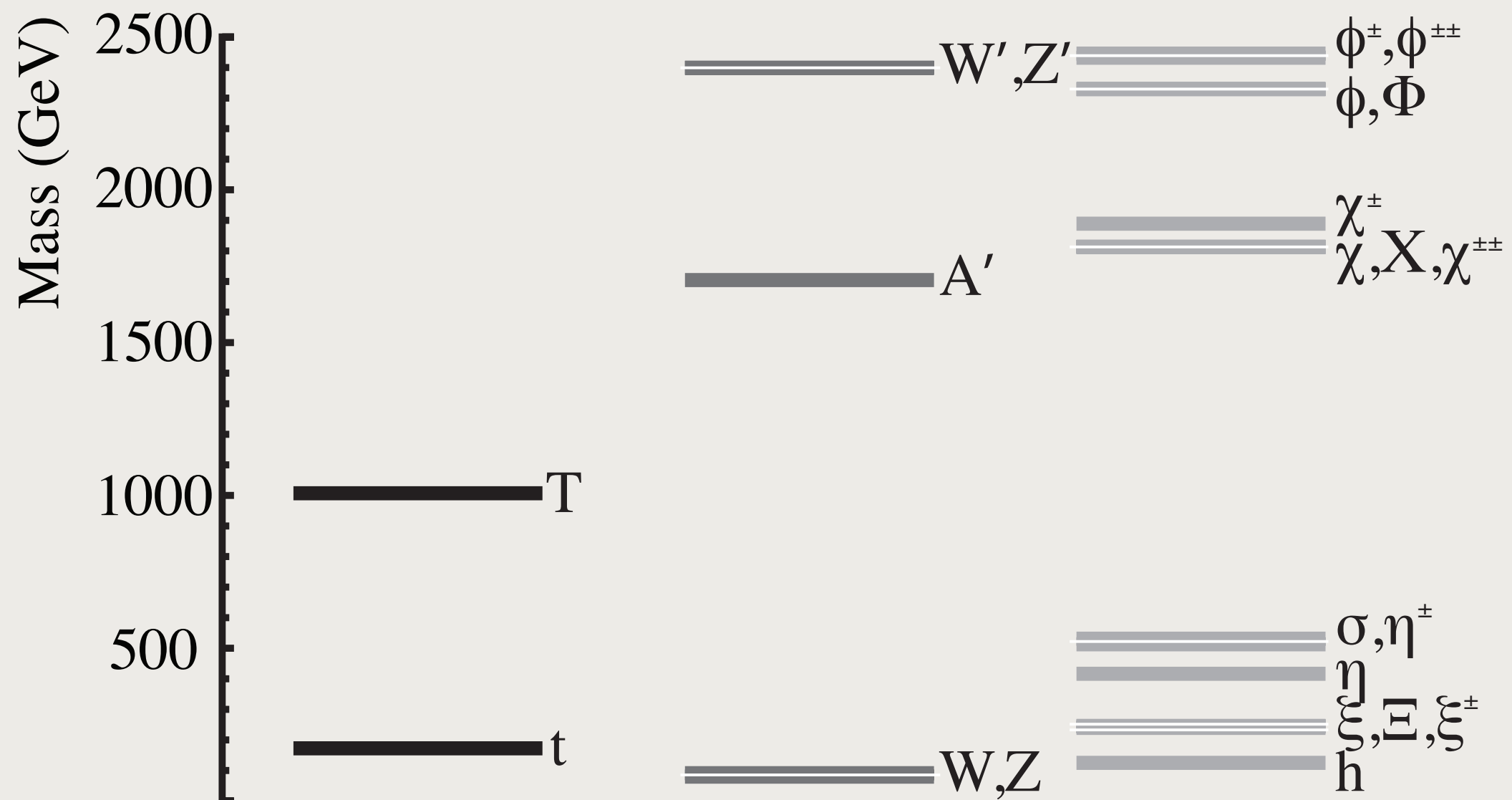
- $\lambda_5$  term not generated from CW potential

$$V_{\Sigma\Delta} = -\lambda_{\Sigma\Delta} f^2 F^2 \text{Tr} [T_{\Sigma\Delta} (\Sigma - \Sigma_0) T_{\Sigma\Delta} (\Delta - \Delta_0)^\dagger] + \text{h.c.}$$

- $T_{\Sigma\Delta} = n_1 \text{Diag}[1, 1, 0, 0, 0] + n_2 \text{Diag}[0, 0, 0, 1, 1]$
- Need  $\text{DM}_\xi > \text{few hundred keV}$ , so  $l_{SD}$  small  
( $\lambda_{\Sigma\Delta} = 0.02 \rightarrow \text{DM}_\xi \sim \text{few GeV}$ )

# Phenomenology of NLH

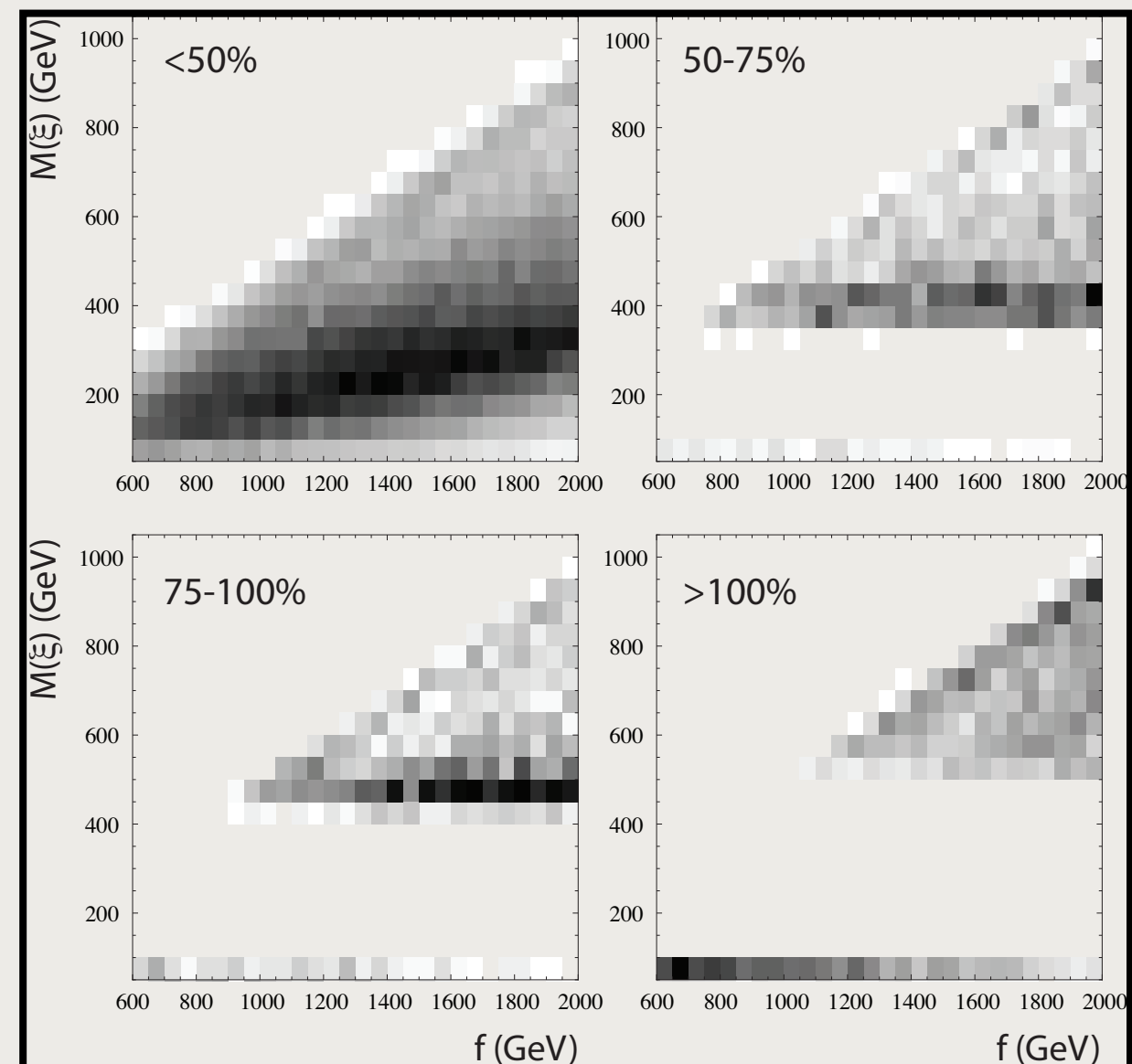
## ● Sample spectrum



# Phenomenology of NLH

- $\Omega h^2 = 0.1189$  (Planck results) arXiv:1303.5076
- Monte Carlo parameters & use MicrOMEGAs
- 130k parameter sets:

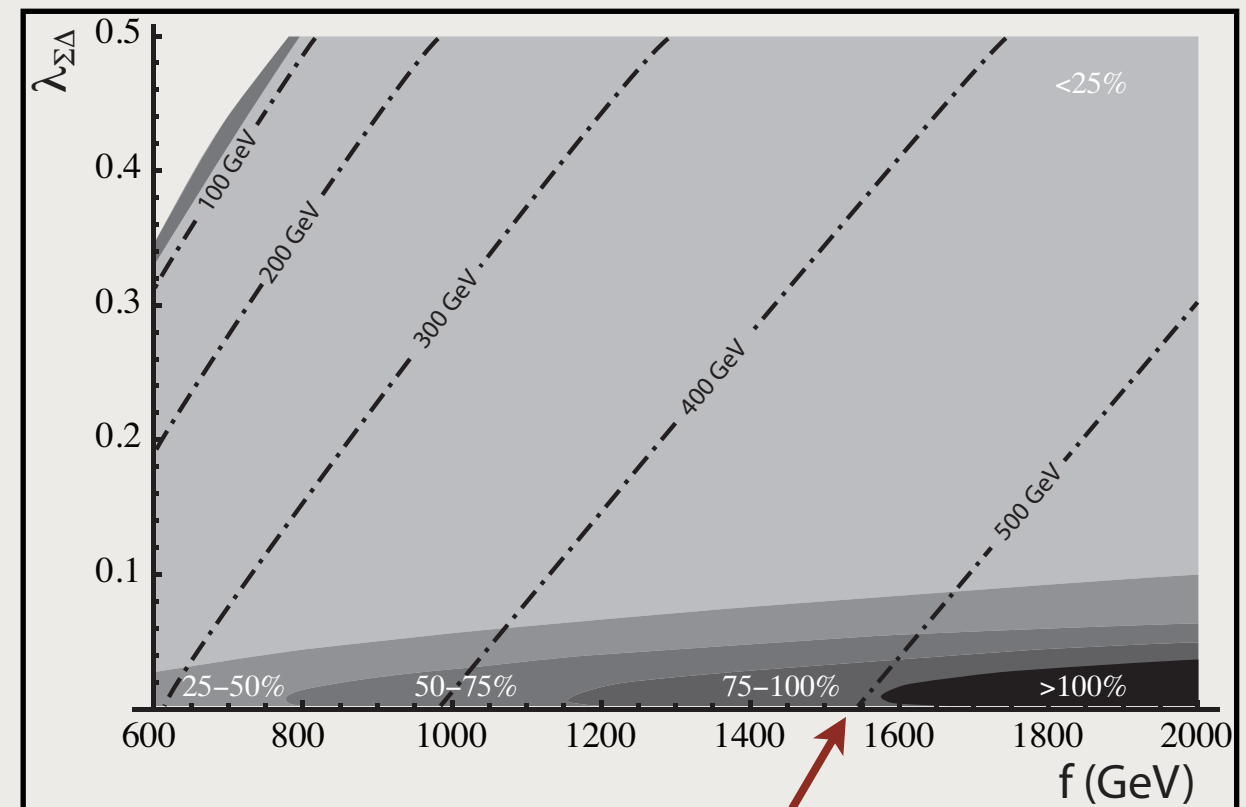
$\Omega h^2 / \Omega h^2_{Planck}$	Events
0%–25%	61%
25%–50%	4.4%
50%–75%	2.0%
75%–100%	1.2%
> 100%	2.6%
N/A	28.8%



# Phenomenology of NLH

- Fix all parameters, vary  $f$  &  $\lambda_{\Sigma\Delta}$

- $s=0.24, s'=0.24$
- $s_t=0.25$
- $F=3000$  GeV
- $a=1, a'=1$



$M_\xi = 505$  GeV

- $f=1550$  GeV

- $\lambda_{\Sigma\Delta}=0.02 \rightarrow \text{DM}_\xi = 4.7$  GeV

- $\Omega h^2 = 0.116$

$$\xi\xi \rightarrow ZZ : 77.3\%$$

$$\xi\xi \rightarrow hh : 19.1\%$$

$$\xi\xi \rightarrow t\bar{t} : 3.5\%$$

- New class of Little Higgs models
- Motivates Inert Doublet models
- Can account for full relic abundance with  $\sim 500$  GeV dark matter
- Relax precision constraints

- Acknowledgements
  - 
  - Heather Logan
  - Thomas Grégoire
  - David Morrissey

# Backup Slides



# Littlest Higgs Model

- $SU(5)/SO(5)$ , breaking at scale  $f \sim O(\text{TeV})$
- Gauge  $[SU(2) \times U(1)]^2$
- One loop log:  $m^2 h^2$

$$\mu^2 = \frac{\lambda}{16\pi^2} M_\phi^2 \log \frac{\Lambda^2}{M_\phi^2} + \frac{3}{64\pi^2} \left( 3g^2 M_{W'}^2 \log \frac{\Lambda^2}{M_{W'}^2} + g'^2 M_{B'}^2 \log \frac{\Lambda^2}{M_{B'}^2} \right) - \frac{3\lambda_t^2}{8\pi^2} m_T^2 \log \frac{\Lambda^2}{m_T^2}$$

- New particle content:
  - Vector quark –  $T$
  - Gauge partners –  $A_H, Z_H, W_H^\pm$
  - Scalars –  $f^0, f^\pm, f^{\pm\pm}$



# Littlest Higgs with T-Parity

- T-Parity:  $Z_2$  symmetry  $g_1 = g_2$   
 $g_1' = g_2'$
- T-Even:
  - $H, W^\pm, Z, g, u/d/e/n, Q_+$
- T-Odd:
  - $f, W_H^\pm, Z_H, A_H, Q_-$
- Triplet vev forbidden
- Avoid precision constraints from  $W_H/Z_H$

# Positive Singlet Mass

- $M_s^2 < 0$ , leads to singlet vev (bad!)
- Introduce new term:

$$V_\Delta = \lambda_\Delta F^4 \text{Tr} [T_\Delta (\Delta - \Delta_0) T_\Delta (\Delta - \Delta_0)^\dagger]$$

- $T_D = \text{Diag}[0, 0, 1, 0, 0]$